# Table, Tabby, Tortoise Problem 

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This is a cute little problem I came across via James Tanton ${ }^{1}$ on Twitter by Ayush DM: ${ }^{2}$

Here is an old Watsapp problem. How high is the table? Also find the height of the cat and tortoise.

## My Solution

Using Figure 1 to translate the problem to symbolic algebra, where $\mathrm{H}, \mathrm{C}$, and T represent the heights of the table, cat, and tortoise respectively, we get the following two equations.

$$
\begin{aligned}
& \mathrm{H}-\mathrm{T}+\mathrm{C}=34 \\
& \mathrm{H}-\mathrm{C}+\mathrm{T}=26
\end{aligned}
$$

Adding the two equations yields

$$
2 \mathrm{H}=60 \Rightarrow \mathrm{H}=30 \mathrm{in}
$$

So the table is 30 inches high.


Figure 1 Problem Statement

If we subtract the two equations, we get

$$
2(\mathrm{C}-\mathrm{T})=8 \Rightarrow \mathrm{C}=\mathrm{T}+4
$$

This means any height for the cat (less than the table height of 30 inches) is allowable, so long at the tortoise's height is 4 inches less. So there is not a unique solution for the heights of the cat and tortoise.

## Alternate Solution

Ayush DM's Twitter site posted a more visual solution by Miguel $\mathrm{HH}^{3}$ as shown in Figure 2.

[^0]

Figure 2 Alternative, Visual Solution by M1GU3LL $\mathbb{H} \mathbb{H}$
Clearly, this is a clever solution. The straight algebraic solution seems pedestrian by contrast. But that is just the point. Translating a problem into symbolic algebra and then (mindlessly?) solving it by the rules of algebra should be straight-forward and available to anyone who has studied algebra. There is no need for clever, ad hoc insights, however fun and surprising these may be. That means a powerful tool for solving problems is available to anyone, and not just geniuses. How great is that?


[^0]:    ${ }^{1} \mathrm{https}: / /$ twitter.com/jamestanton/status/ 1261139105611567106 [spoiler alert]
    ${ }_{2} \mathrm{https}: / /$ twitter.com/AYUSHDM1/status/1261085250928570369
    $3 \mathrm{https}: / /$ twitter.com/M1GU3L_HH/status/1261169101034196993/photo/1

